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#### **Key Points:**

- Integral fluxes (fluences) of four extreme solar particle events (ESPEs) are reconstructed using a novel multiproxy approach
- ESPE fluences are shown to have a spectral shape similar to the most powerful modern solar particle events but orders of magnitude greater
- For the reconstruction, we used recent cosmogenic isotope measurements combined with state-of-the-art modeling

#### **Supporting Information:**

Supporting Information may be found in the online version of this article.

#### Correspondence to:

S. Koldobskiy, sergey.koldobskiy@oulu.fi

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## Multiproxy Reconstructions of Integral Energy Spectra for Extreme Solar Particle Events of 7176 BCE, 660 BCE, 775 CE, and 994 CE

#### Sergey Koldobskiy<sup>1</sup>, Florian Mekhaldi<sup>2,3</sup>, Gennady Kovaltsov<sup>4</sup>, and Ilya Usoskin<sup>1</sup>

<sup>1</sup>Space Physics and Astronomy Research Unit and Sodankylä Geophysical Observatory, University of Oulu, Oulu, Finland, <sup>2</sup>Department of Geology-Quaternary Sciences, Lund University, Lund, Sweden, <sup>3</sup>British Antarctic Survey, Ice Dynamics and Paleoclimate, Cambridge, UK, <sup>4</sup>Ioffe Physical-Technical Institute RAS, St. Petersburg, Russia

**Abstract** Extreme solar particle events (ESPEs) are rare and the most potent known processes of solar eruptive activity. During ESPEs, a vast amount of cosmogenic isotopes (CIs) <sup>10</sup>Be, <sup>36</sup>Cl, and <sup>14</sup>C can be produced in the Earth's atmosphere and deposited in natural stratified archives. Accordingly, CI measurements in these archives allow us to evaluate particle fluxes during ESPEs. In this work, we present a new method of ESPE fluence (integral flux) reconstruction based on state-of-the-art modeling advances, allowing to fit together different CI data within one model. We represent the ESPE fluence as an ensemble of scaled fluence reconstructions for ground-level enhancement (GLE) events registered by the neutron monitor network since 1956 coupled with satellite and ionospheric measurements data. Reconstructed ESPE fluences appear softer in its spectral shape than earlier estimates, leading to significantly higher estimates of the low-energy (*E* < 100 MeV) fluence. This makes ESPEs even more dangerous for modern technological systems than previously believed. Reconstructed ESPE fluences are fitted with a modified Band function, which eases the use of obtained results in different applications.

#### 1. Introduction

The only quantitative way to study solar and the related cosmic-ray variabilities over long time scales beyond the era of direct measurements is through cosmogenic isotopes (CIs, see, e.g., Beer et al., 2012; Usoskin, 2017) which are produced in the Earth's atmosphere by cosmic rays and then are stored in natural independently dateable stratified archives (tree rings, ice cores, sediments, etc.) from where they can be extracted and measured in modern laboratories (e.g., Brehm et al., 2021; Vonmoos et al., 2006). The most important CIs for solar and cosmic-ray studies are  ${}^{14}C$  (aka radiocarbon) measured in dendrochronologically dated tree rings, as well as  ${}^{10}Be$  and  ${}^{36}Cl$ . both measured in glaciologically dated polar ice cores. These CIs are normally produced by an omnipresent but variable flux of galactic cosmic rays (GCRs), forming the main proxy data set for long-term solar-activity reconstructions (e.g., Bard et al., 2000; Muscheler et al., 2007; Solanki et al., 2004; Steinhilber et al., 2012; Usoskin et al., 2021; Wu et al., 2018). Sporadic solar energetic particle (SEP) events usually cannot produce a detectable amount of CIs (Mekhaldi et al., 2021; Usoskin, Koldobskiy, Kovaltsov, Rozanov, et al., 2020; Usoskin, Solanki, Kovaltsov, et al., 2006), but very seldom, roughly once per millennium, extremely strong solar particle events (called ESPEs henceforth) take place, with the SEP event-integrated flux (fluence) exceeding that of "usual" SEP events by several orders of magnitude (e.g., Cliver et al., 2022). Such events can lead to significant spikes in the cosmogenic-isotope production that can be detected by accelerator mass spectrometry, AMS (e.g., Miyake et al., 2019; Synal & Wacker, 2010). The first such spike, dated to 775 CE, was discovered in 2012 by Miyake et al. (2012) and soon was confirmed to be an ESPE (Usoskin et al., 2013). Since then, three more ESPEs have been confirmed (i.e., independently found in several sources), dated to 994 CE, 660 BCE, and 7176 BCE (Brehm et al., 2022; Miyake et al., 2013; O'Hare et al., 2019; Paleari et al., 2022; Park et al., 2017). In addition, four ESPE candidates, in 5410 BCE, 5259 BCE, 1052 CE, and 1279 CE (Brehm et al., 2022; Miyahara et al., 2022; Miyake et al., 2021) are waiting for independent confirmation.

Since ESPEs form a type of extremely strong solar eruptive events never observed directly with scientific instrumentation, and may represent new, presently unknown, physical processes on the Sun (Usoskin & Kovaltsov, 2021), it is crucially important to assess their characteristic parameters, specifically, the energy spectrum. Generally, the event-integrated spectrum can be estimated based on data from different isotopes for the same event: <sup>14</sup>C and <sup>10</sup>Be isotopes are effectively sensitive to SEP with the energy above 230 MeV while the effective energy



of SEPs producing <sup>36</sup>Cl is much lower, about 60 MeV (Koldobskiy et al., 2022). Recently, several approaches have been used to evaluate the spectra of the ESPEs. The spectra of ESPEs of 775 CE and 994 CE (Mekhaldi et al., 2015) as well as around 660 BCE (O'Hare et al., 2019) were estimated by using the relationship between the <sup>36</sup>Cl/<sup>10</sup>Be ratio and SEP spectral hardness of SEP-induced ground level enhancements (GLEs) registered by ground-based neutron monitor (NM) network (Usoskin, Koldobskiy, Kovaltsov, Gil, et al., 2020). In both studies, the measured <sup>10</sup>Be and <sup>36</sup>Cl concentrations from Greenland ice cores were compared with modeled production rates induced by modern GLEs, using their spectra and CI production function estimated by Webber et al. (2007). The modern GLE yielding the closest <sup>36</sup>Cl/<sup>10</sup>Be ratio to those measured for the ESPEs was selected and scaled up by using the prescribed, nearly power-law spectral shape form (Webber et al., 2007), leading to very hard energy spectra. Later, Usoskin, Koldobskiy, Kovaltsov, Rozanov, et al. (2020) postulated that the energy spectrum of the ESPE of 775 CE can be represented by a scaled spectrum of the strongest directly observed hard-spectrum SEP event of 23 February 1956 (GLE #5). Similarly to Mekhaldi et al. (2015) and O'Hare et al. (2019), Paleari et al. (2022) leveraged the <sup>36</sup>Cl/<sup>10</sup>Be ratio from the ice-core measurements during the 7176 BCE ESPE to infer the spectral hardness. However, they did so by combining recent production functions (Poluianov et al., 2016) and GLE spectral fluence reconstructions (Koldobskiy et al., 2021; Raukunen et al., 2018), so that the reconstructed spectrum resulted from an ensemble of modern GLE events. Their reconstructed ESPE spectrum appears softer than those assessed earlier (Mekhaldi et al., 2015; O'Hare et al., 2019) and close to that assessed by Usoskin, Koldobskiy, Kovaltsov, Rozanov, et al. (2020).

Here, we develop this approach further and present a systematic reconstruction of integral fluences (event-integrated fluxes) for four ESPEs: 994 CE, 775 CE, 660 BCE, and 7176 BCE, using a newly developed method based on a simultaneous fit of the spectral shape to the measured data of all the three CIs.

#### 2. Data Sources

Here, we use two data sources related to SEP events: cosmogenic-isotope data for ESPEs during the past millennia, and direct observations of SEP events during the recent decades by spacecraft and NMs—GLEs.

#### 2.1. CI Data

Here, we used data of CIs <sup>10</sup>Be, <sup>14</sup>C, and <sup>36</sup>Cl published for four ESPEs of 7176 BCE, 660 BCE, 775 CE, and 994 CE (the dates here are related to the year of the isotope concentration peaks, while the ESPEs could have occurred in the previous calendar year). Details and references to the data are given in Table 1. We carefully selected the data for analysis. In details, for <sup>10</sup>Be measured for ESPE 775 CE, we used reanalysis from Mekhaldi et al. (2021) which supersedes that of Mekhaldi et al. (2015) and includes the data from NEEM, NGRIP, and WAIS ice cores, while measurements at TUNU (Sigl et al., 2015) and Dome F (Miyake et al., 2015) sites were not included since they are noisier rendering their interpretation more ambiguous (Mekhaldi et al., 2021). For the ESPE of 660 BCE, we used NGRIP data which is of annual resolution (and, therefore, better accuracy) unlike the poorer resolved GRIP data. The isotope production by SEPs during an ESPE is quantified as the global production for <sup>14</sup>C and polar deposition flux for <sup>10</sup>Be and <sup>36</sup>Cl, using the parameterization of atmospheric transport and deposition (Heikkilä et al., 2009, 2013).

The isotope production due to ESPE,  $Q_{\text{ESPE}}$ , can be inferred from measurement data as an excess of the production rate Q above the background due to GCR,  $Q_{\text{GCR}}$ . Ideally, from the values of  $Q_{\text{ESPE}}$ , one could directly estimate the parameters of SEPs. This works well for <sup>14</sup>C which is globally mixed and whose production is modeled precisely (Kovaltsov et al., 2012). However, <sup>10</sup>Be and <sup>36</sup>Cl are subjected to a complicated transport and deposition (Field et al., 2006; Golubenko et al., 2021; Heikkilä et al., 2013) dominated by the local/regional effects on short time scales (Pedro et al., 2006; Usoskin et al., 2009; Zheng et al., 2020). Because of that, there is an unknown scaling factor k, typically ranging from 0.8 to 1.3 between the modeled and measured production/deposition rates, related to the local/regional depositional factors (Sukhodolov et al., 2017). This k-factor is a free parameter and cannot be found from the data alone. Because of this, a conversion between the production rate and the SEP spectrum becomes uncertain at a ±20% level. To avoid that, the so-called peak factor P is often used as an index of the ESPE strength (e.g., Mekhaldi et al., 2015) that is the ratio of the measured isotope's production/deposition excess  $Q_{\text{ESPE}}$  to the background annual isotope's production/deposition rate  $Q_{\text{GCR}}$  before and after the ESPE

 $P_{\rm ESPE} = Q_{\rm ESPE} / Q_{\rm GCR}.$ 

(1)



Data and Corresponding Geomagnetic/Heliospheric Conditions for the ESPEs (Represented by Horizontal Blocks) Considered in This Work

	$M_{\rm K}$	$M_{ m P}$	$\phi$	Data				
Event	$(10^{22}  \mathrm{A} \cdot \mathrm{m}^2)$	$(10^{22}  \mathrm{A \cdot m^2})$	(MV)	Source	Туре	<sup>10</sup> Be	<sup>36</sup> Cl	$^{14}C$
994 CE	$10.3 \pm 0.4$	9 ± 0.5	$410 \pm 100$	M15	Р	$1.2 \pm 0.2$	$2.6 \pm 0.3$	$2.40 \pm 0.70$
				B18	Р			$1.80 \pm 0.40$
				B18	Q			$1.04 \pm 0.10$
				B22	Q			$1.18 \pm 0.10$
775 CE	$10.7\pm0.4$	$9.3 \pm 0.5$	$525 \pm 100$	M15	Р		$6.3 \pm 0.4$	$3.90 \pm 0.70$
				B18	Р			$3.20 \pm 0.20$
				B18	Q			$1.88 \pm 0.10$
				M21	Р	$3.0 \pm 0.3$		
				B22	Q			$2.21 \pm 0.10$
660 BCE	$11.4 \pm 0.6$	$9 \pm 0.4$	$390 \pm 100$	O19	Р	$2.5\pm0.9$	$6.4 \pm 1.4$	
				S20	Q			$1.40 \pm 0.10$
				B22	Q			$1.62 \pm 0.2$
7176 BCE	8.7 ± 1.7	$7.5 \pm 0.4$	$550 \pm 100$	P22	Р	$3.7 \pm 0.4$	$6.1 \pm 1.2$	$4.50 \pm 0.50$
				B22	Q			$2.42 \pm 0.1$

*Note.* Columns  $M_{\rm k}$  and  $M_{\rm p}$  represent VADM reconstructions, for the time of the events, by Knudsen et al. (2008) and Panovska et al. (2018), respectively.  $\phi$  is solar modulation potential (see text). "Data source" column specifies the data sources (see text for details): M15—Mekhaldi et al. (2015), B18—Büntgen et al. (2018), O19—O'Hare et al. (2019), S20—Sakurai et al. (2020), M21—Mekhaldi et al. (2021), P22—Paleari et al. (2022), B22—Brehm et al. (2022). "Type" represents the type of data (see text for details), viz., P—P peak ratio, and Q—production (in units of 10<sup>8</sup> cm<sup>-2</sup>).

Under the assumption that the *k*-factor is the same for SEP-produced and GCR-produced isotope atoms, the *P* ratio appears free of the *k*-factor eliminating the related uncertainty. Additionally, a ratio between background concentration and peak concentration can be used for the same purpose, neglecting uncertainties of translation from measured concentration to deposition flux. Ideally, the data of  ${}^{36}$ Cl and  ${}^{10}$ Be should be taken from the same ice core, which is not always possible. Accordingly, new precise measurements (especially for  ${}^{36}$ Cl) are needed for the further progress in ESPE reconstructions.

In this work, we used the measured ratio P for <sup>10</sup>Be and <sup>36</sup>Cl as a quantitative index of the ESPE strength. For <sup>14</sup>C, if  $Q_{\text{ESPE}}$ -values were published, we converted them to the *P*-values using Equation 1 during the fluence reconstruction procedure (details are given in Section 3).

#### 2.2. Direct Data: GLEs Since 1956

Thousands of SEP events, including weak ones, have been directly measured in situ by spacecraft during the recent decades (Desai & Giacalone, 2016; Vainio et al., 2013), but only several tens of them were sufficiently strong and energetic to initiate a nucleonic cascade in the Earth's atmosphere and thus potentially produce CIs. However, the directly observed SEP events for the last 70 years were unable to produce a detectable amount of CIs (Mekhaldi et al., 2021; Usoskin, Koldobskiy, Kovaltsov, Rozanov, et al., 2020). Strongest SEP events were registered by ground-based neutrons monitors (NMs) as GLE events (Usoskin, Koldobskiy, Kovaltsov, Gil, et al., 2020) that serve as reference events for ESPEs (Mekhaldi et al., 2021; Usoskin, Koldobskiy, Kovaltsov, Rozanov, et al., 2020). SEP spectral fluences (event-integrated and energy-integrated fluxes) from ~30 MeV to several GeVs have been recently reconstructed for 58 moderate and strong GLE events by Koldobskiy et al. (2021) based on a combination of ground-based and space-borne data sets. Here, we used these spectral reconstructions as an ensemble of reference spectra, similarly to Mekhaldi et al. (2021) and Paleari et al. (2022).

The highest typically achievable time resolution for paleo-events (including ESPEs) is 1 year, or seasonal at best. Considering also the response time of CI, i.e., the time between the production of CI, on one hand, and



Table 2

List of C

GLE Events	Considered Here

GLE(s)	Date	GLE(s)	Date
5	23/02/1956	38	07/12/1982
8	04/05/1960	39	16/02/1984
10-12	Nov. 1960	40	25/07/1989
13	18/07/1961	41	15/08/1989
16	28/01/1967	42-45	OctNov. 1989
18	29/09/1968	46	15/11/1989
19	18/11/1968	47–50	May 1990
20	25/02/1969	51–52	Jun 1990
21	30/03/1969	53	25/06/1992
22	24/01/1971	55	06/11/1997
23	01/09/1971	56	02/05/1998
24–25	Aug. 1972	58	24/08/1998
26	29/04/1973	59	14/07/2000
27	30/04/1976	60–61	Apr. 2001
28–29	Sep. 1977	62	04/11/2001
30	22/11/1977	63	26/12/2001
31	07/05/1978	64	24/08/2002
32	23/09/1978	65–67	OctNov. 2003
33	21/08/1979	69	20/01/2005
35	10/05/1981	70	13/12/2006
36	12/10/1981	71	16/05/2012
37	26/11/1982	72	10/09/2017

the uptake by trees for <sup>14</sup>C (e.g., Beer et al., 2012; Usoskin et al., 2013) or deposition of <sup>10</sup>Be and <sup>36</sup>Cl in Greenland and Antarctica ice cores (Heikkilä et al., 2009), on the other hand, of 1–2 years, the CI method cannot distinguish between a single extreme event and a series of consequent events as, e.g., in October– November 1989. Accordingly, for further analysis, we have combined "serial" GLEs produced by the same solar active region into pseudo-single GLE events with the summed spectral fluences. The list of the considered GLEs (single and serial) is given in Table 2.

For each GLE event, the integral omnidirectional fluence F (in units of cm<sup>-2</sup>) was parameterized over rigidity R with the modified Band function (MBF), which is a double power-law with an exponential roll-off (Koldobskiy et al., 2021)

$$F(>R) = J_1 \left(\frac{R}{1 \text{ GV}}\right)^{-\gamma_1} \exp\left(-\frac{R}{R_1}\right) \text{ if } R < R_b,$$
  

$$F(>R) = J_2 \left(\frac{R}{1 \text{ GV}}\right)^{-\gamma_2} \exp\left(-\frac{R}{R_2}\right) \text{ if } R \ge R_b$$
(2)

where  $\gamma_1$ ,  $R_1$ ,  $J_1$ ,  $\gamma_2$ ,  $R_2$  are parameters of the fit and R is the particle's rigidity in GV. Parameters  $\gamma_0$ ,  $R_b$ , and  $J_1$  can be calculated using other parameters

$$\gamma_0 = \gamma_2 - \gamma_1$$

$$R_0 = R_1 \cdot R_2 / (R_2 - R_1)$$

$$R_b = \gamma_0 \cdot R_0$$

$$J_1 = J_2 \cdot R_b^{-\gamma_0} \cdot \exp(\gamma_0)$$
(3)

The MBF can be analytically differentiated yielding the differential flux of SEPs over rigidity  $dF/(dR d\Omega) \equiv J$  (in units of cm<sup>-2</sup> GV<sup>-1</sup> sr<sup>-1</sup>) assuming the isotropic SEP flux

$$J(R) = \frac{1}{4\pi} J_1 \left(\frac{R}{1 \text{ GV}}\right)^{-\gamma_1} \exp\left(-\frac{R}{R_1}\right) \left(\frac{\gamma_1}{R} + \frac{1}{R_1}\right) \text{ if } R < R_b,$$
  

$$J(R) = \frac{1}{4\pi} J_2 \left(\frac{R}{1 \text{ GV}}\right)^{-\gamma_2} \exp\left(-\frac{R}{R_2}\right) \left(\frac{\gamma_2}{R} + \frac{1}{R_2}\right) \text{ if } R \ge R_b$$
(4)

These differential fluxes are used for computations of the CI production as described in Section 2.3.

#### 2.3. Modeling of Production and Deposition of CIs

For a comparison with the measured data, we computed the modeled production of CIs in the Earth's atmosphere using the approach based on the yield functions (Poluianov et al., 2016). This allowed us to compute the CI production in the atmosphere, but the measured data include also atmospheric transport and deposition. Radiocarbon (<sup>14</sup>C) is usually taken as globally mixed in the atmosphere and then involved in the global carbon cycle, often modeled by a "multibox" model (e.g., Büntgen et al., 2018). For <sup>10</sup>Be and <sup>36</sup>Cl, the measured quantity is concentration in ice, which is sometimes subsequently translated, via the snow accumulation rate, into the depositional flux which is related to the atmospheric production via transport and deposition processes, we used the "effective" yield functions  $Y_{\rm eff}$  which account for the global production of <sup>14</sup>C and production + transport + polar deposition for <sup>10</sup>Be and <sup>36</sup>Cl (Asvestari, Gil, et al., 2017; Asvestari, Willamo, et al., 2017; Koldobskiy et al., 2022).

For the GCR-based production, we modeled the GCR spectrum using the broadly used force-field approximation (e.g., Caballero-Lopez & Moraal, 2004) applying the local interstellar spectrum of GCRs according to Vos and Potgieter (2015), constructed to fit both low-energy data from Voyager satellites at the outer heliospheric boundary and higher-energy data from modern PAMELA and AMS-02 satellites. Heavier (Z > 1) nuclei were



considered following the approach described in Koldobskiy et al. (2019). The force-field model includes only one variable parameter, the modulation potential  $\phi$  (see the methodology in, e.g., Usoskin et al. (2005)). There have been many estimates of the modulation potential in the past (e.g., Vonmoos et al., 2006; Steinhilber et al., 2012) but they are not always intercomparable because the modulation potential is a slightly model-dependent quantity (Herbst et al., 2010; Usoskin et al., 2005). For consistency, here, we use the values of  $\phi$  corresponding to the times of ESPEs as obtained or reconstructed using the same methodology from Usoskin et al. (2021) for ESPE 994 CE, from Sukhodolov et al. (2017) for 775 CE, and from Wu et al. (2018) for the times of 660 BCE and 7176 BCE. The collected  $\phi$ -values, along with their uncertainties, are presented in column 4 of Table 1.

Since the flux of cosmic rays, both GCRs and SEPs, near Earth is modulated also by the geomagnetic field, whose intensity and directions slowly change in time, it is essential to consider a realistic geomagnetic field during the times of ESPEs. The geomagnetic shielding of charged particles is mostly affected by the dipole component of the geomagnetic field (e.g., Nevalainen et al., 2013) which is often quantified in terms of the virtual dipole moment (VDM) or, typically for paleomagnetic reconstructions, the virtual axial dipole moment (VADM—see, e.g., Usoskin, Solanki, & Korte, 2006), denoted henceforth as *M*. Here, we considered two archeo/ paleomagnetic shielding during the times of ESPEs, by Knudsen et al. (2008) and by Panovska et al. (2018), the VADM values being denoted as  $M_{\rm K}$  and  $M_{\rm P}$ , respectively, to cover the full range of uncertainties. The collected *M*-values, along with their uncertainties, are presented in columns 2 and 3 of Table 1.

Using the effective yield functions, the measured quantities of the CIs (Section 2.1) produced by cosmic rays of the given origin (GCR or SEP) can be calculated as

$$Q(t) = \sum_{l} \int_{0}^{\infty} J_{l}(R, t) \cdot Y_{\text{eff},l}(R, M(t)) \cdot dR$$
(5)

where the summation is over types of cosmic-ray particles (proton,  $\alpha$ -particles, heavier species),  $J_l(R, t)$  is the differential rigidity spectrum of the *l*th specie at moment *t*,  $Y_{\text{eff},l}(R, M)$  is the effective yield function for the particle of type *l*, M(t) is the VADM value, and the integration is over the rigidity.

#### 3. Spectral Reconstruction

The procedure of the reconstruction of the spectral fluence for individual ESPEs is based on an iterative Monte-Carlo approach as described below in consecutive steps.

- 1. For a given ESPE, a set of the experimental cosmogenic proxy data along with their uncertainties was selected from Table 1. The data sources were chosen randomly and independently for each isotope (e.g., M21, M15, and B18 could be randomly selected for <sup>10</sup>Be, <sup>36</sup>Cl, and <sup>14</sup>C, respectively, for the 775 CE event). In this way, a set of three CI measurements of ESPE peak factors and their uncertainties (both marked with index *i* to denote different CIs) were selected.
- 2. For each GLE (single or "serial") listed in Table 2, we simulated its differential fluence in the form of MBF (Equation 4), where the exact values of parameters were randomly (with the normally distributed pseudo-random numbers with zero mean and unity variance) taken from the uncertainty range as reported in Table 2 of Koldobskiy et al. (2021). Accordingly, we obtain a set of SEP differential spectra J<sub>j</sub>, where j is the number of individual or "serial" GLE events as listed in Table 2.
- 3. For each SEP differential flux  $J_j$ , obtained at step 2 above, we calculated the expected <sup>14</sup>C global production and deposition fluxes of <sup>10</sup>Be and <sup>36</sup>Cl, viz.  $Q_{i,j}^*$ , using Equation 5. The geomagnetic shielding was modeled for each ESPE with the VADM value  $M^*$  being simulated using a normally distributed pseudo-random number r(zero mean, unity variance) as  $M^* = M + r \cdot \sigma_M$ , where M and  $\sigma_M$  are taken from Table 1. In addition, it was simulated randomly with the equal probability, whether  $M_K$  or  $M_P$  values are used. The  $M^*$  value was taken the same for the calculation of the SEP-induced production/deposition of all three CIs within one realization.
- 4. Next, we calculated the annual global production (for <sup>14</sup>C) or deposition fluxes (for <sup>10</sup>Be and <sup>36</sup>Cl) of CIs due to GCRs,  $Q^*_{GCR,i}$ , using the  $M^*$  values as obtained at step 3. The exact value of the modulation potential  $\phi^*$  (column 4 in Table 1) was simulated using a normally distributed pseudo-random number as  $\phi^* = \phi + r \cdot \sigma_{\phi}$ . The same value of  $\phi^*$  was used for all isotopes at this step. After that, we calculated the peak factors (see Equation 1) for each individual or "serial" GLE event:  $P^*_{i,i} = Q^*_{i,i}/Q^*_{GCR,i}$ . If the global production data for <sup>14</sup>C



was selected during step 1, we also calculated the <sup>14</sup>C peak factor for the measured data using obtained value of  $Q^*_{\text{con-14c}}$ .

of Q<sup>\*</sup><sub>GCR,<sup>14</sup>C</sub>.
5. For each set of P<sup>\*</sup><sub>i,j</sub> modeled above, we found a scaling factor κ<sub>j</sub> which scales the CIs modeled for the *j*th GLE to match the observed peak factors in CI data. This is quantified via the minimization of the χ<sup>2</sup> merit function

$$\chi_j^2 = \sum_i \left( \frac{\kappa_j \cdot P_{i,j}^* - P_{\text{ESPE},i}}{\sigma_{\text{ESPE},i}} \right)^2 \tag{6}$$

where  $P_{\text{ESPE},i}$  and  $\sigma_{\text{ESPE},i}$  are taken at step 1 from columns 7 to 9 of Table 1 or, for <sup>14</sup>C global production reconstructions, recalculated from Table 1 data using step 4, and the summation is over the three CIs. The best-fit solution of Equation 6 can be found analytically as

$$\kappa_{j} = \frac{\sum P_{i,j}^{*} \cdot P_{\text{ESPE},i} / \sigma_{\text{ESPE},i}^{2}}{\sum \left(\frac{P}{i,j} / \sigma_{\text{ESPE},i}\right)^{2}}$$
(7)

The best-fit scale factors  $\kappa_i$  and the corresponding values of  $\chi_i^2$  were saved for each realization.

Steps 1–5 were repeated in 1,000 realizations and the corresponding matrices of  $\chi_{j,k}^2$ , best-fit scaling factors  $\kappa_{j,k}$  and MBF parameters were collected, where *k* denotes the number of the realization. During this iterative process, all pseudo-random numbers used in the simulations were calculated independently and anew at each step and each realization.

Two additional criteria were then applied for each realization to get a reliable solution:

- Only realizations with the κ ≤ 3,500 were selected to avoid amplification of noise. For example, for the ESPE of 775 CE, realizations with κ > 3,500 roughly correspond to a moderate GLE event with the integral increase of ≤80%\*h as recorded by a polar sea-level NMs.
- Only realizations with χ<sup>2</sup> ≤ 5.99 were selected, as corresponding, with two degrees of freedom, to the *p*-value of 0.05 implying that the considered model fits the data reasonably well (Press et al., 2007).

Realizations passing these selection criteria were used to form an ensemble of "good fits" of the ESPE integral fluence estimates defined as  $F_{ESPE} = \kappa_j F_{GLE,j}$ , where  $F_{GLE,j}$  is the integral fluence of the *j*th GLE computed using the stored MBF parameters. For this ensemble, the median value and the 68% confidence intervals of  $F_{ESPE}$  were calculated for each rigidity, as shown in Figures 1 and 2. Numeric values of reconstructed ESPE fluences F(>E) for selected energies are given in Table 3, and tables with finer energy resolution (10 bins per energy decade) are given as Supporting Information S1.

To check the robustness of ESPE fluence estimates, we also consider the effect of systematic change in M and  $\phi$  values used for reconstruction. Change of M by 10% leads to negligible effect (less than a percent) on the reconstructed median value of ESPE fluences. Change of  $\phi$  by 20% leads to a 2% difference for the reconstructed median value of ESPE fluence at 30 MeV, and the difference fades progressively with energy. Therefore, the proposed method is more robust to uncertainties of  $\phi$  and M in comparison to methods used earlier, because it considers all three isotopes simultaneously and deals with absolute (not only relative) ESPE production of <sup>14</sup>C.

#### 4. Results and Discussion

#### 4.1. Comparison With Other Results

Figure 1 shows the results obtained here along with earlier spectral estimates from Mekhaldi et al. (2015) for ESPEs of 994 CE and 775 CE as well as from Paleari et al. (2022) for ESPE 7176 BCE. As seen in Figure 1, the new spectral reconstruction yields significantly softer spectrum at E > 100 MeV than those estimated earlier by Mekhaldi et al. (2015) for ESPEs of 775 CE and 994 CE. We note that the earlier work was based on a simplified assumption of a prescribed unrealistically hard power-law shape of the SEP spectrum (Webber et al., 2007), prior to the updated fluence spectra reconstructed by Koldobskiy et al. (2021). In addition, the yield function of CI production has been essentially revisited recently (Poluianov et al., 2016). As shown previously by Mekhaldi et al. (2021), this directly transfers into a higher enhancement factor required to explain past ESPEs when comparing to modern GLEs. As such, the fluence >30 MeV of the 775 CE and 994 CE events were reassessed





**Figure 1.** Integral spectral fluences of extreme solar particle events (ESPEs) of 994 CE, 775 CE, 660 BCE, and 7176 BCE (panels a through d, respectively): red/blue/green/violet lines with shaded areas depict the reconstructions presented here (the median and 68% confidence intervals, respectively); orange lines with shaded areas depict the spectral reconstructions by Mekhaldi et al. (2015); greenish vertical bars represent estimates of the  $F_{30}$  fluence by Mekhaldi et al. (2021); black vertical bars in panel d correspond to the spectral estimates by Paleari et al. (2022) for the ESPE of 7176 BCE.

using the more realistic fluence spectra of Raukunen et al. (2018) and assuming a solar modulation function as per Steinhilber et al. (2012) and Vonmoos et al. (2006). These estimates are closer to our new reconstructed fluence spectra in comparison to the first reconstruction (Mekhaldi et al., 2015), but are still significantly lower. We examined the reason for the difference and found out that the spectral estimate by Mekhaldi et al. (2021) was based explicitly on the scaled spectrum of GLE #5 which is the hardest-spectrum known GLE. On the contrary, Paleari et al. (2022) used an ensemble of GLEs as reconstructed by Raukunen et al. (2018) resulting in a softer energy-spectrum reconstruction which is in excellent agreement with our new reconstruction (Figure 1d) based on the revised GLE spectra (Koldobskiy et al., 2021).

Figure 2 depicts integral spectra of the four ESPEs reconstructed here. As seen, three events (775 CE, 660 BCE, and 7176 BCE) are very close to each other within the uncertainties, while the ESPE of 994 CE is a factor 2–3 weaker. For comparison, integral spectra of three "typical" GLEs are also shown as dashed curves: the strongest hard-spectrum GLE #5 (23 February 1956), the strongest soft-spectrum GLE #24 (04 August 1972), and a "typical" spectrum corresponding to a series of GLEs during October–November 1989 (GLE #42–45). One can see that the ESPE spectra are 2 orders of magnitude higher than that of a typical strong GLE. The fact that the CI data can be well fitted with scaled spectra of the observed GLEs implies that the physical mechanisms of acceleration and interplanetary transport of SEPs during ESPEs are similar to those of a "normal" GLE, favoring the idea that ESPEs are *Black swan* (a strong unexpected event whose nature can be understood a posteriori, viz. once it has occurred—Taleb, 2007) rather than *Dragon king* (huge-size unexpected event whose nature cannot be understood, in the framework of the existing knowledge, even after it has occurred—Sornette & Ouillon, 2012) type events (Cliver et al., 2022; Usoskin & Kovaltsov, 2021).

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**Figure 2.** Integral spectral fluences of solar energetic particles (SEPs) reconstructed here for the four extreme solar particle events (ESPEs; solid curves with shaded areas identical to those in Figure 1). Digital data for these curves are available in Table 3. Dashed curves denote integral fluences for three selected GLEs according to Koldobskiy et al. (2021): the hard-spectrum GLE #5 (blue), soft-spectrum GLE #24 (orange), and a "typical" GLE #42–45 (green), as denoted in the legend.

#### 4.2. Parameterization of the Spectra

Different applications, e.g., calculation of the CI response (Equation 5), require knowledge of not the integral flux (fluence), but differential-in-energy particle flux. For this purpose, we fitted integral spectra of ESPEs reconstructed here with the MBF spectral form (Equation 2), which can be easily differentiated (Equation 4). The MBF fitting procedure was based on the Monte-Carlo iterative approach. The initial guess for the MBF parameter values corresponded to GLE #5 as described in Koldobskiy et al. (2021). For each iteration, the exact values of MBF parameters ( $\gamma_1$ ,  $R_1$ ,  $J_2$ ,  $\gamma_2$ ,  $R_2$ ) were randomly and independently chosen using the normal distribution (with  $\sigma$  of 10% of the parameter value). Each obtained fit parameter set was checked to be mathematically reasonable, so the fit function should not have a positive derivative anywhere, since the integral fluence cannot increase with R. This condition was quantified as  $\gamma_1/R + 1/R_1 > 0$  for the rigidity range  $R < R_b$ . For a chosen set of parameters, we have calculated expected fluence values  $F_{\text{fit},i}$  using 10 logarithmic bins per 1 order of magnitude in energy range spanning from 30 MeV to 10 GeV. After that, we assessed the agreement between fit and reconstructed ESPE fluences using  $\chi^2$  merit function

$$\chi^{2} = \sum_{i} \left( \frac{F_{\text{ESPE},i} - F_{\text{fit},i}}{\sigma_{\text{ESPE},i}} \right)^{2}$$
(8)

where the summation is over bins described above,  $F_{\text{ESPE}}$  are fluence values for these energy bins, and  $\sigma_{\text{ESPE}}$  are corresponding 68% confidence intervals.

Table 3         Reconstructed ESPE Fluences in Units of cm <sup>-2</sup>							
ESPE	$F_{30} \cdot 10^{-11}$	$F_{60} \cdot 10^{-11}$	$F_{100} \cdot 10^{-10}$	$F_{200} \cdot 10^{-10}$	$F_{300} \cdot 10^{-9}$	$F_{600}\cdot 10^{-9}$	$F_{1000} \cdot 10^{-8}$
994 CE	$1.16^{+0.41}_{-0.53}$	$0.39^{+0.10}_{-0.07}$	$1.72^{+0.32}_{-0.30}$	$0.46^{+0.08}_{-0.07}$	$1.87^{+0.43}_{-0.29}$	$0.33^{+0.07}_{-0.08}$	$0.70^{+0.24}_{-0.24}$
775 CE	$2.42^{+0.68}_{-0.69}$	$0.94^{+0.18}_{-0.19}$	$4.13^{+0.63}_{-0.61}$	$1.09^{+0.15}_{-0.13}$	$4.29^{+0.82}_{-0.60}$	$0.73^{+0.16}_{-0.16}$	$1.49^{+0.50}_{-0.37}$
660 BCE	$2.41^{+1.65}_{-1.07}$	$0.99^{+0.37}_{-0.31}$	$4.38^{+1.07}_{-0.97}$	$1.15^{+0.16}_{-0.14}$	$4.54_{-0.63}^{+0.84}$	$0.78^{+0.20}_{-0.22}$	$1.62^{+0.58}_{-0.64}$
7176 BCE	$1.62^{+0.50}_{-0.72}$	$0.78^{+0.17}_{-0.35}$	$4.01^{+0.88}_{-1.64}$	$1.28^{+0.25}_{-0.29}$	$5.67^{+0.87}_{-0.74}$	$1.05_{-0.20}^{+0.45}$	$2.15^{+2.60}_{-0.47}$



**Table 4**Best-Fit MBF (Equation 2) Parameters Along With  $1\sigma$  Uncertainties for theESPE Fluences Reconstructed Here

ESPE	$\gamma_1$	$R_1$ (GV)	$J_1 ({\rm cm}^{-2})$	$\gamma_2$	$R_2$ (GV)
994 CE	$2.18^{+0.95}_{-2.78}$	$0.42^{+0.60}_{-0.32}$	$\left(1.25^{+1.44}_{-0.45} ight)\cdot10^9$	$3.93^{+1.82}_{-0.96}$	$2.11^{+3.83}_{-1.23}$
775 CE	$1.65^{+1.02}_{-1.95}$	$0.28^{+0.41}_{-0.19}$	$\left(2.98^{+3.35}_{-1.18} ight)\cdot10^9$	$3.85^{+1.52}_{-0.80}$	$1.78^{+3.47}_{-0.99}$
660 BCE	$1.57^{+1.30}_{-2.40}$	$0.27^{+0.49}_{-0.19}$	$\left(3.27^{+3.98}_{-1.41} ight)\cdot10^9$	$3.77^{+1.75}_{-0.85}$	$1.70^{+3.15}_{-0.94}$
7176 BCE	$1.33^{+0.84}_{-1.89}$	$0.35^{+0.38}_{-0.22}$	$\left(3.51^{+5.14}_{-1.15}\right)\cdot10^9$	$4.36^{+1.16}_{-1.73}$	$3.69^{+6.12}_{-2.62}$

If the value of  $\chi_j^2$  for the *j*th iteration appears smaller than the previous ones, it was saved as  $\chi_{\min}^2$ , the corresponding MBF parameters were considered as a new initial guess set, and the iteration counter was reset.

The procedure was repeated 1 million times. In addition to the best-fit values, corresponding to  $\chi^2_{min}$ , we also calculated the  $1\sigma$  uncertainty of the MBF parameters considering the parameter-value sets, for which  $\chi^2 \le \chi^2_{min} + 5.89$ . The procedure was repeated for all GLEs MBF parameters listed in Koldobskiy et al. (2021) and minimal value of  $\chi^2$  and corresponding MBF parameters were saved. Thus obtained best-fit MBF parameters for ESPE fluence fitting together with 68% c.i. uncertainties are given in Table 4. MBF parameters are interrelated, the example of their mutual distributions and also

the dependence of  $\chi^2$  for best-fit (red dot) and 68% c.i. interval (blue dots) is shown in Figure 3 for the event 775 CE. Other ESPEs demonstrate similar parameter interrelation and quality of the fit.

#### 4.3. Expected NM Response to ESPE

We also investigated quantitatively the possible NM response to an ESPE should it occur now under the single event hypothesis. The strength of a GLE event can be quantified with the integral relative increase I, measured in %-hours, of a sea-level polar NM count rate caused by SEPs above the GCR background (Asvestari, Gil, et al., 2017; Asvestari, Willamo, et al., 2017; Usoskin, Koldobskiy, Kovaltsov, Gil, et al., 2020). The greatest known integral increase of NM count rate of 5,300%\*h was registered during GLE #5 by Ottawa NM (subpolar sea-level NM). We have calculated NM integral increase due to ESPEs using the yield function approach (Equation 5) utilizing the NM yield function calculated by Mishev et al. (2020). For assessment of GCR background we took LIS by Vos and Potgieter (2015), consideration of heavy elements from Koldobskiy et al. (2019) and solar modulation potential values from Table 1. Three events of similarly high magnitude (775 CE, 660 BCE, and 7176 BCE) were taken as reference events. We took MBF fit parameter realizations within 68% c.i. for each of considered events and calculated the expected NM response to these events for a polar sea-level NM (geomagnetic cutoff rigidity  $P_c = 0$  GV, atmospheric depth h = 1,000 g/cm<sup>2</sup>). The estimated integral increase I was found in the range from ~75,000 to ~280,000%\*h, which is a factor ~15–50 greater than GLE #5. Such a strong enhancement of the count rate (a typical count rate of a NM64 is about 10 counts/s/counter) would likely cause a saturation of a real NM considering the standard dead-time of the standard NM read-out electronics of 2 milliseconds.

#### 5. Conclusions

A new quantitative nonparametric multiproxy method of the reconstruction of integral fluences is presented as based on the scaling of the existing GLE spectra to match the available cosmogenic-isotope data for each event. This allowed us to consistently reconstruct integral fluxes of all four extreme solar particle events for which all three CIs are currently measured. The method utilizes a Monte Carlo approach to find the most probable solution in the form of the scaled directly observed GLE spectra and to estimate the uncertainties. The combination of the newly revisited, more robust GLE spectra estimates (Koldobskiy et al., 2021) and an updated CI production function (Poluianov et al., 2016) used for the reconstruction yielded an order-of-magnitude higher fluence of lower energy <100 MeV relative to the original estimates for the 994 CE, 775 CE, and 660 BCE ESPEs. The result obtained here for EPSE 7176 BCE is in good agreement with the recent reconstruction by Paleari et al. (2022).

SEPs with energies E < 100 MeV are most dangerous for technological and health hazards (e.g., Miyake et al., 2019) so new ESPE fluence reconstructions allow a better assessment of the potential impact of ESPE on modern society.

Statistically justified opportunity to describe ESPE integral flux with scaled spectra of typical strong GLE events recorded during the recent decades implies that ESPEs are likely produced by a mechanism similar to that of the "regular" GLEs. This suggests that ESPE are likely *Black-swan* events whose origin can be understood in terms of the existing knowledge (Cliver et al., 2022; Usoskin & Kovaltsov, 2021).

The spectral shape of the four analyzed events appears similar to one another. Interestingly, while the event of 994 CE is somewhat smaller, the other three ESPEs have very similar intensities. Since it is unlikely that



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Figure 3. Interrelation of modified Band function (MBF) parameters and their dependence on  $\chi^2$  for extreme solar particle event (ESPE) 775 CE. Red dot corresponds to best-fit solution, other points are within 68% c.i.

significantly stronger ESPEs could be found over the Holocene (Cliver et al., 2022; Miyake et al., 2019), this could be speculated as an upper limit of the SEP events produced by the Sun. However, more data including the detection of new ESPEs, confirmation of existing candidates and their fluence reconstructions are required to prove that.

In conclusion, a new method, based on cosmogenic-isotope proxy, for the robust nonparametric reconstruction of integral energy spectra for ESPE has been proposed and applied to four ESPEs detected over the last millennia, viz. 7176 BCE, 660 BCE, 775 CE, and 994 CE. The reconstructed ESPE spectral fluences have been parameterized in the form of the modified Band function. This result provides new insight into the physics of rare extreme solar events on the multimillennial time scale.

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### **Data Availability Statement**

Data used for ESPE reconstructions are available elsewhere.

- CI ESPE measurements: Mekhaldi et al. (2015), Büntgen et al. (2018), O'Hare et al. (2019), Sakurai et al. (2020), Mekhaldi et al. (2021), Paleari et al. (2022), and Brehm et al. (2022).
- VADM reconstructions: Knudsen et al. (2008) and Panovska et al. (2018).
- GLE reconstructions: Koldobskiy et al. (2021).
- CI yield functions: Poluianov et al. (2016), Asvestari, Gil, et al. (2017).
- solar modulation potential reconstruction: Sukhodolov et al. (2017), Wu et al. (2018), and Usoskin et al. (2021).

ESPE fluences with fine energy resolution are available in the Supporting Information S1 to this paper.

#### References

- Asvestari, E., Gil, A., Kovaltsov, G. A., & Usoskin, I. G. (2017). Neutron monitors and cosmogenic isotopes as cosmic ray energy-integration detectors: Effective yield functions, effective energy, and its dependence on the local interstellar spectrum. *Journal of Geophysical Research:* Space Physics, 122, 9790–9802. https://doi.org/10.1002/2017JA024469
- Asvestari, E., Willamo, T., Gil, A., Usoskin, I. G., Kovaltsov, G. A., Mikhailov, V. V., & Mayorov, A. (2017). Analysis of Ground Level Enhancements (GLE): Extreme solar energetic particle events have hard spectra. *Advances in Space Research*, 60(4), 781–787. https://doi. org/10.1016/j.asr.2016.08.043
- Bard, E., Raisbeck, G., Yiou, F., & Jouzel, J. (2000). Solar irradiance during the last 1200 years based on cosmogenic nuclides. *Tellus Series B: Chemical and Physical Meteorology*, 52(3), 985–992. https://doi.org/10.1034/j.1600-0889.2000.d01-7.x
- Beer, J., McCracken, K., & von Steiger, R. (2012). Cosmogenic radionuclides: Theory and applications in the terrestrial and space environments. Springer. Retrieved from https://link.springer.com/book/10.1007/978-3-642-14651-0
- Brehm, N., Bayliss, A., Christl, M., Synal, H.-A., Adolphi, F., Beer, J., et al. (2021). Eleven-year solar cycles over the last millennium revealed by radiocarbon in tree rings. *Nature Geoscience*, 14(1), 10–15. https://doi.org/10.1038/s41561-020-00674-0
- Brehm, N., Christl, M., Knowles, T. D. J., Casanova, E., Evershed, R. P., Adolphi, F., et al. (2022). Tree-rings reveal two strong solar proton events in 7176 and 5259 BCE. *Nature Communications*, 13(1), 1196. https://doi.org/10.1038/s41467-022-28804-9
- Büntgen, U., Wacker, L., Galván, J. D., Arnold, S., Arseneault, D., Baillie, M., et al. (2018). Tree rings reveal globally coherent signature of cosmogenic radiocarbon events in 774 and 993 CE. *Nature Communications*, 9(1), 3605. https://doi.org/10.1038/s41467-018-06036-0
- Caballero-Lopez, R., & Moraal, H. (2004). Limitations of the force field equation to describe cosmic ray modulation. *Journal of Geophysical Research*, 109, A01101. https://doi.org/10.1029/2003JA010098
- Cliver, E. W., Schrijver, C. J., Shibata, K., & Usoskin, I. (2022). Extreme solar events. Living Reviews in Solar Physics, 19(1), 2. https://doi.org/10.1007/s41116-022-00033-8
- Desai, M., & Giacalone, J. (2016). Large gradual solar energetic particle events. *Living Reviews in Solar Physics*, 13(1), 3. https://doi.org/10.1007/ s41116-016-0002-5
- Field, C., Schmidt, G., Koch, D., & Salyk, C. (2006). Modeling production and climate-related impacts on <sup>10</sup>Be concentration in ice cores. *Journal of Geophysical Research*, 111, D15107. https://doi.org/10.1029/2005JD006410
- Golubenko, K., Rozanov, E., Kovaltsov, G., Leppänen, A.-P., Sukhodolov, T., & Usoskin, I. (2021). Application of CCM SOCOL-AERv2-BE to cosmogenic beryllium isotopes: Description and validation for polar regions. *Geoscientific Model Development*, 14(12), 7605–7620. https:// doi.org/10.5194/gmd-14-7605-2021
- Harris, C. R., Millman, K. J., van der Walt, S. J., Gommers, R., Virtanen, P., Cournapeau, D., et al. (2020). Array programming with NumPy. *Nature*, 585(7825), 357–362. https://doi.org/10.1038/s41586-020-2649-2
- Heikkilä, U., Beer, J., Abreu, J. A., & Steinhilber, F. (2013). On the atmospheric transport and deposition of the cosmogenic radionuclides (<sup>10</sup>Be): A review. *Space Science Reviews*, 176(1–4), 321–332. https://doi.org/10.1007/s11214-011-9838-0
- Heikkilä, U., Beer, J., & Feichter, J. (2009). Meridional transport and deposition of atmospheric <sup>10</sup>Be. Atmospheric Chemistry and Physics, 9(2), 515–527. https://doi.org/10.5194/acp-9-515-2009
- Herbst, K., Kopp, A., Heber, B., Steinhilber, F., Fichtner, H., Scherer, K., & Matthiä, D. (2010). On the importance of the local interstellar spectrum for the solar modulation parameter. *Journal of Geophysical Research*, 115, D00I20. https://doi.org/10.1029/2009JD012557
- Hunter, J. D. (2007). Matplotlib: A 2D graphics environment. Computing in Science & Engineering, 9(3), 90–95. https://doi.org/10.1109/ MCSE.2007.55
- Knudsen, M. F., Riisager, P., Donadini, F., Snowball, I., Muscheler, R., Korhonen, K., & Pesonen, L. J. (2008). Variations in the geomagnetic dipole moment during the Holocene and the past 50 kyr. *Earth and Planetary Science Letters*, 272(1–2), 319–329. https://doi.org/10.1016/j. epsl.2008.04.048
- Koldobskiy, S. A., Bindi, V., Corti, C., Kovaltsov, G. A., & Usoskin, I. G. (2019). Validation of the neutron monitor yield function using data from AMS-02 experiment, 2011–2017. Journal of Geophysical Research: Space Physics, 124, 2367–2379. https://doi.org/10.1029/2018JA026340
- Koldobskiy, S. A., Raukunen, O., Vainio, R., Kovaltsov, G. A., & Usoskin, I. (2021). New reconstruction of event-integrated spectra (spectral fluences) for major solar energetic particle events. Astronomy & Astrophysics, 647, A132. https://doi.org/10.1051/0004-6361/202040058
  Koldobskiy, S. A., Usoskin, I., & Kovaltsov, G. A. (2022). Effective energy of cosmogenic isotope (<sup>10</sup>Be, <sup>14</sup>C and <sup>36</sup>Cl) produc-
- tion by solar energetic particles and galactic cosmic rays. *Journal of Geophysical Research: Space Physics*, 127, e2021JA029919. https://doi.org/10.1029/2021JA029919
- Kovaltsov, G., Mishev, A., & Usoskin, I. (2012). A new model of cosmogenic production of radiocarbon <sup>14</sup>C in the atmosphere. *Earth and Planetary Science Letters*, 337, 114–120. https://doi.org/10.1016/j.epsl.2012.05.036
- Mekhaldi, F., Adolphi, F., Herbst, K., & Muscheler, R. (2021). The signal of solar storms embedded in cosmogenic radionuclides: Detectability and uncertainties. *Journal of Geophysical Research: Space Physics, 126*, e2021JA029351. https://doi.org/10.1029/2021JA029351
- Mekhaldi, F., Muscheler, R., Adolphi, F., Aldahan, A., Beer, J., McConnell, J. R., et al. (2015). Multiradionuclide evidence for the solar origin of the cosmic-ray events of AD 774/5 and 993/4. *Nature Communications*, 6(1), 8611. https://doi.org/10.1038/ncomms9611

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- Mishev, A. L., Koldobskiy, S. A., Kovaltsov, G. A., Gil, A., & Usoskin, I. G. (2020). Updated neutron-monitor yield function: Bridging between in situ and ground-based cosmic ray measurements. *Journal of Geophysical Research: Space Physics*, 125, e2019JA027433. https://doi. org/10.1029/2019JA027433
- Miyahara, H., Tokanai, F., Moriya, T., Takeyama, M., Sakurai, H., Ohyama, M., et al. (2022). Recurrent large-scale solar proton events before the onset of the wolf grand solar minimum. *Geophysical Research Letters*, 49, e2021GL097201. https://doi.org/10.1029/2021GL097201
- Miyake, F., Masuda, K., & Nakamura, T. (2013). Another rapid event in the carbon-14 content of tree rings. *Nature Communications*, 4(1), 1748. https://doi.org/10.1038/ncomms2783
- Miyake, F., Nagaya, K., Masuda, K., & Nakamura, T. (2012). A signature of cosmic-ray increase in ad 774–775 from tree rings in Japan. Nature, 486(7402), 240–242. https://doi.org/10.1038/nature11123
- Miyake, F., Panyushkina, I. P., Jull, A. J. T., Adolphi, F., Brehm, N., Helama, S., et al. (2021). A single year cosmic ray event at 5410 BCE registered in 14C of tree rings. *Geophysical Research Letters*, 48, e2021GL093419. https://doi.org/10.1029/2021GL093419
- Miyake, F., Suzuki, A., Masuda, K., Horiuchi, K., Motoyama, H., Matsuzaki, H., et al. (2015). Cosmic ray event of A.D. 774-775 shown in quasi-annual <sup>10</sup>Be data from the Antarctic Dome Fuji ice core. *Geophysical Research Letters*, 42, 84–89. https://doi.org/10.1002/2014GL062218
   Miyake, F., Usoskin, I., & Poluianov, S. (Eds.) (2019). *Extreme solar particle storms: The hostile sun.* IOP Publishing. https://doi.

org/10.1088/2514-3433/ab404a

- Muscheler, R., Joos, F., Beer, J., Müller, S. A., Vonmoos, M., & Snowball, I. (2007). Solar activity during the last 1000 yr inferred from radionuclide records. *Quaternary Science Reviews*, 26(1–2), 82–97. https://doi.org/10.1016/j.quascirev.2006.07.012
- Nevalainen, J., Usoskin, I. G., & Mishev, A. (2013). Eccentric dipole approximation of the geomagnetic field: Application to cosmic ray computations. Advances in Space Research, 52(1), 22–29. https://doi.org/10.1016/j.asr.2013.02.020
- O'Hare, P., Mekhaldi, F., Adolphi, F., Raisbeck, G., Aldahan, A., Anderberg, E., et al. (2019). Multiradionuclide evidence for an extreme solar proton event around 2,610 B.P. (~660 BC). Proceedings of the National Academy of Sciences of the United States of America, 116(13), 5961–5966. https://doi.org/10.1073/pnas.1815725116

Paleari, C. I., Mekhaldi, F., Adolphi, F., Christl, M., Vockenhuber, C., Gautschi, P., et al. (2022). Cosmogenic radionuclides reveal an extreme solar particle storm near a solar minimum 9125 years BP. *Nature Communications*, 13(1), 214. https://doi.org/10.1038/s41467-021-27891-4 Pandas development team T. (2020). pandas-dev/pandas: Pandas. *Zenodo*. https://doi.org/10.5281/zenodo.3509134

- Panovska, S., Constable, C. G., & Korte, M. (2018). Extending global continuous geomagnetic field reconstructions on timescales beyond human civilization. Geochemistry, Geophysics, Geosystems, 19, 4757–4772. https://doi.org/10.1029/2018GC007966
- Park, J., Southon, J., Fahrni, S., Creasman, P. P., & Mewaldt, R. (2017). Relationship between solar activity and 14C peaks in AD 775, AD 994, and 660 BC. *Radiocarbon*, 59(4), 1147–1156. https://doi.org/10.1017/rdc.2017.59
- Pedro, J., van Ommen, T., Curran, M., Morgan, V., Smith, A., & McMorrow, A. (2006). Evidence for climate modulation of the 10Be solar activity proxy. *Journal of Geophysical Research*, 111, D21105. https://doi.org/10.1029/2005JD006764
- Poluianov, S. V., Kovaltsov, G. A., Mishev, A. L., & Usoskin, I. G. (2016). Production of cosmogenic isotopes <sup>7</sup>Be, <sup>10</sup>Be, <sup>14</sup>C, <sup>22</sup>Na, and <sup>36</sup>Cl in the atmosphere: Altitudinal profiles of yield functions. *Journal of Geophysical Research: Atmospheres*, *121*, 8125–8136. https://doi.org/10.1002/2016JD025034
- Press, W. H., Teukolsky, S. A., Vetterling, W. T., & Flannery, B. P. (2007). Numerical recipes: The art of scientific computing. Cambridge University Press.
- Raukunen, O., Vainio, R., Tylka, A. J., Dietrich, W. F., Jiggens, P., Heynderickx, D., et al. (2018). Two solar proton fluence models based on ground level enhancement observations. *Journal of Space Weather and Space Climate*, 8, A04. https://doi.org/10.1051/swsc/2017031
- Sakurai, H., Tokanai, F., Miyake, F., Horiuchi, K., Masuda, K., Miyahara, H., et al. (2020). Prolonged production of 14C during the ~660 BCE solar proton event from Japanese tree rings. *Scientific Reports*, 10(1), 660. https://doi.org/10.1038/s41598-019-57273-2
- Sigl, M., Winstrup, M., McConnell, J. R., Welten, K. C., Plunkett, G., Ludlow, F., et al. (2015). Timing and climate forcing of volcanic eruptions for the past 2,500 years. *Nature*, 523(7562), 543–549. https://doi.org/10.1038/nature14565
- Solanki, S. K., Usoskin, I. G., Kromer, B., Schüssler, M., & Beer, J. (2004). Unusual activity of the Sun during recent decades compared to the previous 11,000 years. *Nature*, 431(7012), 1084–1087. https://doi.org/10.1038/nature02995
- Sornette, D., & Ouillon, G. (2012). Dragon-kings: Mechanisms, statistical methods and empirical evidence. The European Physical Journal Special Topics, 205(1), 1–26. https://doi.org/10.1140/epjst/e2012-01559-5
- Steinhilber, F., Abreu, J., Beer, J., Brunner, I., Christl, M., Fischer, H., et al. (2012). 9,400 years of cosmic radiation and solar activity from ice cores and tree rings. Proceedings of the National Academy of Sciences of the United States of America, 109(16), 5967–5971. https://doi. org/10.1073/pnas.1118965109
- Sukhodolov, T., Usoskin, I., Rozanov, E., Asvestari, E., Ball, W. T., Curran, M. A., et al. (2017). Atmospheric impacts of the strongest known solar particle storm of 775 AD. Scientific Reports, 7, 45257. https://doi.org/10.1038/srep45257
- Synal, H.-A., & Wacker, L. (2010). AMS measurement technique after 30 years: Possibilities and limitations of low energy systems. Nuclear Instruments and Methods in Physics Research Section B, 268(7–8), 701–707. https://doi.org/10.1016/j.nimb.2009.10.009

Taleb, N. (2007). The black swan: The impact of the highly improbable. Random House.

- Usoskin, I. (2017). A history of solar activity over millennia. Living Reviews in Solar Physics, 14(1), 3. https://doi.org/10.1007/s41116-017-0006-9
  Usoskin, I., Alanko-Huotari, K., Kovaltsov, G. A., & Mursula, K. (2005). Heliospheric modulation of cosmic rays: Monthly reconstruction for 1951–2004. Journal of Geophysical Research, 110, A12108. https://doi.org/10.1029/2005JA011250
- Usoskin, I. G., Horiuchi, K., Solanki, S., Kovaltsov, G. A., & Bard, E. (2009). On the common solar signal in different cosmogenic isotope data sets. Journal of Geophysical Research, 114, A03112. https://doi.org/10.1029/2008JA013888
- Usoskin, I., Koldobskiy, S., Kovaltsov, G., Gil, A., Usoskina, I., Willamo, T., & Ibragimov, A. (2020). Revised GLE database: Fluences of solar energetic particles as measured by the neutron-monitor network since 1956. Astronomy & Astrophysics, 640, A17. https://doi. org/10.1051/0004-6361/202038272
- Usoskin, I., Koldobskiy, S., Kovaltsov, G., Rozanov, E., Sukhodolov, T., Mishev, A., & Mironova, I. (2020). Revisited reference solar proton event of 23-Feb-1956: Assessment of the cosmogenic-isotope method sensitivity to extreme solar events. *Journal of Geophysical Research: Space Physics*, 125, e2020JA027921. https://doi.org/10.1029/2020JA027921
- Usoskin, I., & Kovaltsov, G. (2021). Mind the gap: New precise <sup>14</sup>C data indicate the nature of extreme solar particle events. *Geophysical Research Letters*, 48, e2021GL094848. https://doi.org/10.1029/2021GL094848
- Usoskin, I., Kromer, B., Ludlow, F., Beer, J., Friedrich, M., Kovaltsov, G. A., et al. (2013). The AD775 cosmic event revisited: The Sun is to blame. *Astronomy & Astrophysics*, 552, L3. https://doi.org/10.1051/0004-6361/201321080
- Usoskin, I., Solanki, S., Kovaltsov, G., Beer, J., & Kromer, B. (2006). Solar proton events in cosmogenic isotope data. *Geophysical Research Letters*, 33, L08107. https://doi.org/10.1029/2006GL026059



- Usoskin, I., Solanki, S. K., & Korte, M. (2006). Solar activity reconstructed over the last 7000 years: The influence of geomagnetic field changes. *Geophysical Research Letters*, 33, L08103. https://doi.org/10.1029/2006GL025921
- Usoskin, I., Solanki, S. K., Krivova, N. A., Hofer, B., Kovaltsov, G. A., Wacker, L., et al. (2021). Solar cyclic activity over the last millennium reconstructed from annual <sup>14</sup>C data. *Astronomy & Astrophysics*, 649, A141. https://doi.org/10.1051/0004-6361/202140711
- Vainio, R., Valtonen, E., Heber, B., Malandraki, O. E., Papaioannou, A., Klein, K.-L., et al. (2013). The first SEPServer event catalogue ~68-MeV solar proton events observed at 1 AU in 1996-2010. *Journal of Space Weather and Space Climate*, *3*, A12. https://doi.org/10.1051/ swsc/2013030
- Virtanen, P., Gommers, R., Oliphant, T. E., Haberland, M., Reddy, T., Cournapeau, D., et al. (2020). SciPy 1.0: Fundamental algorithms for scientific computing in Python. *Nature Methods*, 17(3), 261–272. https://doi.org/10.1038/s41592-019-0686-2
- Vonmoos, M., Beer, J., & Muscheler, R. (2006). Large variations in Holocene solar activity: Constraints from <sup>10</sup>Be in the Greenland ice core project ice core. *Journal of Geophysical Research*, 111, A10105. https://doi.org/10.1029/2005JA011500
- Vos, E. E., & Potgieter, M. S. (2015). New modeling of galactic proton modulation during the minimum of solar cycle 23/24. The Astrophysical Journal, 815(2), 119. https://doi.org/10.1088/0004-637X/815/2/119
- Webber, W., Higbie, P., & McCracken, K. (2007). Production of the cosmogenic isotopes <sup>3</sup>H, <sup>7</sup>Be, <sup>10</sup>Be, and <sup>36</sup>Cl in the Earth's atmosphere by solar and galactic cosmic rays. *Journal of Geophysical Research*, *112*, A10106. https://doi.org/10.1029/2007JA012499
- Wu, C. J., Usoskin, I. G., Krivova, N., Kovaltsov, G. A., Baroni, M., Bard, E., & Solanki, S. K. (2018). Solar activity over nine millennia: A consistent multi-proxy reconstruction. Astronomy & Astrophysics, 615, A93. https://doi.org/10.1051/0004-6361/201731892
- Zheng, M., Adolphi, F., Sjolte, J., Aldahan, A., Possnert, G., Wu, M., et al. (2020). Solar and climate signals revealed by seasonal <sup>10</sup>Be data from the NEEM ice core project for the neutron monitor period. *Earth and Planetary Science Letters*, 541, 116273. https://doi.org/10.1016/j.epsl.2020.116273